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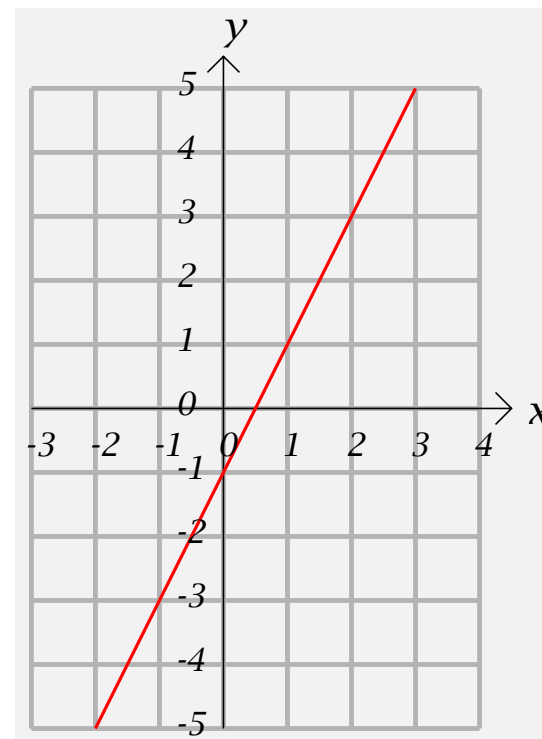
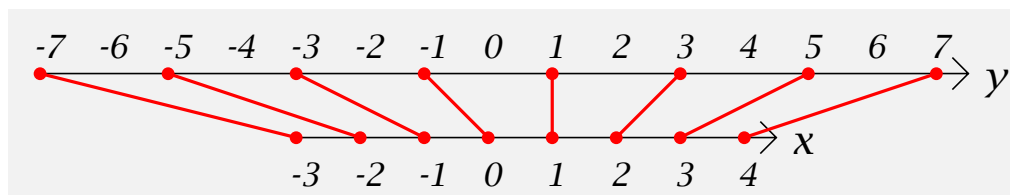
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x	-3	-2	-1	0	1	2	3	4
$f(x)$	-7	-5	-3	-1	1	3	5	7



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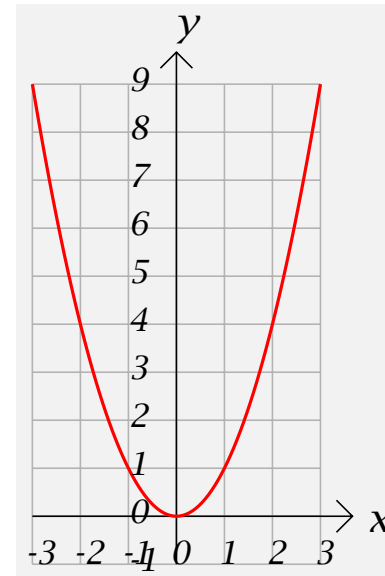
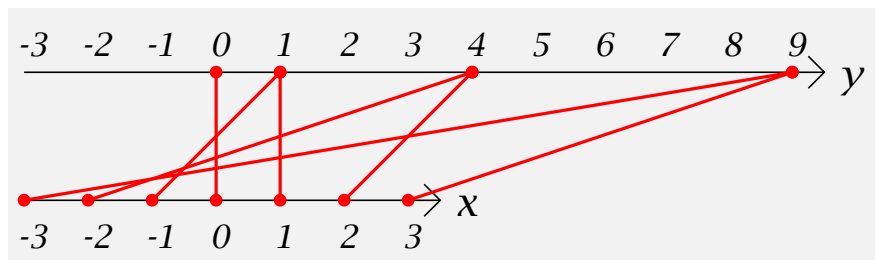
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$f(x)$	9	4	1	0	1	4	9



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